

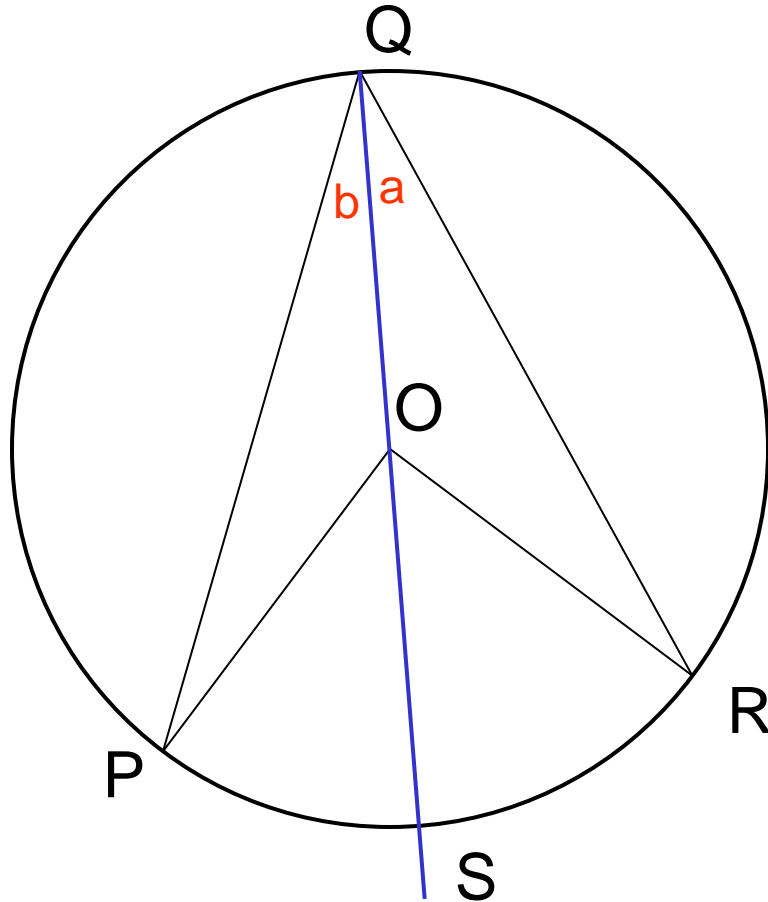
# Proof

## Circle Theorems

# Contents

- Angle at Centre
- Opposite angles in cyclic quadrilateral
- Alternate Segment Theorem

# Prove angle at centre is twice the angle at the circumference



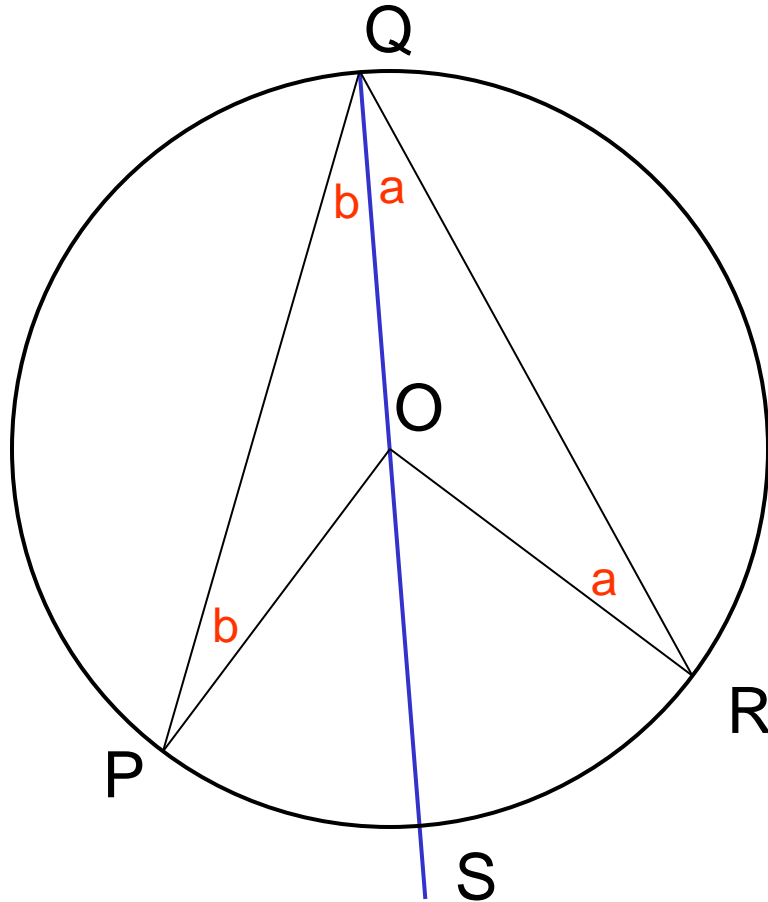
Draw line QO and extend to intersect circumference at S

Label angles

$\angle OQR$  is **a**

$\angle OQP$  is **b**

# Prove angle at centre is twice the angle at the circumference



$$\angle ORQ = \angle OQR$$

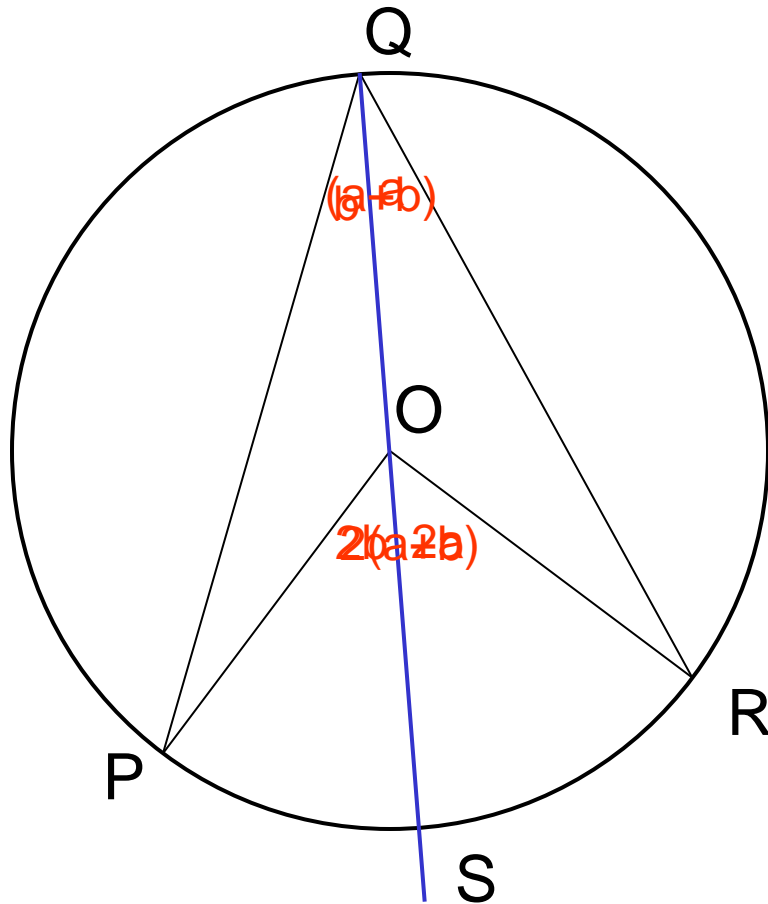
Base angles in Isosceles Triangle  
( $OQ = OR$ , radii of circle)

Similarly

$$\angle OPQ = \angle OQP$$



# Prove angle at centre is twice the angle at the circumference



$$\begin{aligned}\angle POR &= 2a + 2b \\ &= 2(a + b)\end{aligned}$$

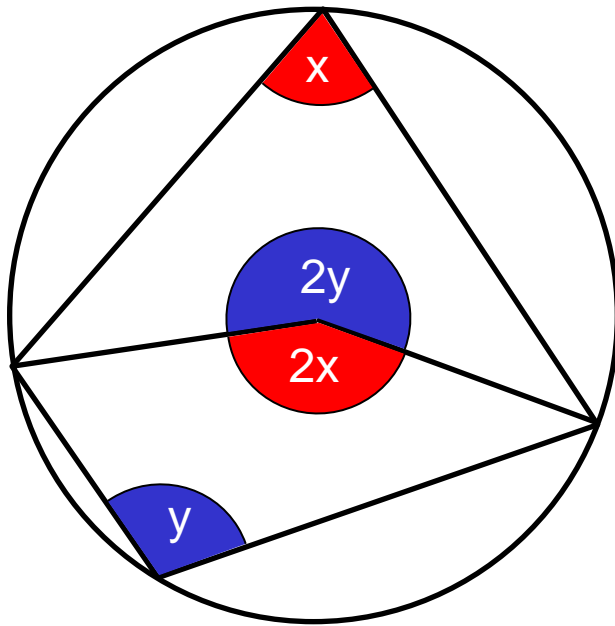
$$\angle PQR = a + b$$

$$\angle POR = 2 \times \angle PQR$$

Return to Menu

# Opposite Angles in a Cyclic Quadrilateral are supplementary

Required to Prove that  $x + y = 180^\circ$



Draw in radii

The angle at the centre is  
TWICE the angle at the  
circumference

$$2x + 2y = 360^\circ$$

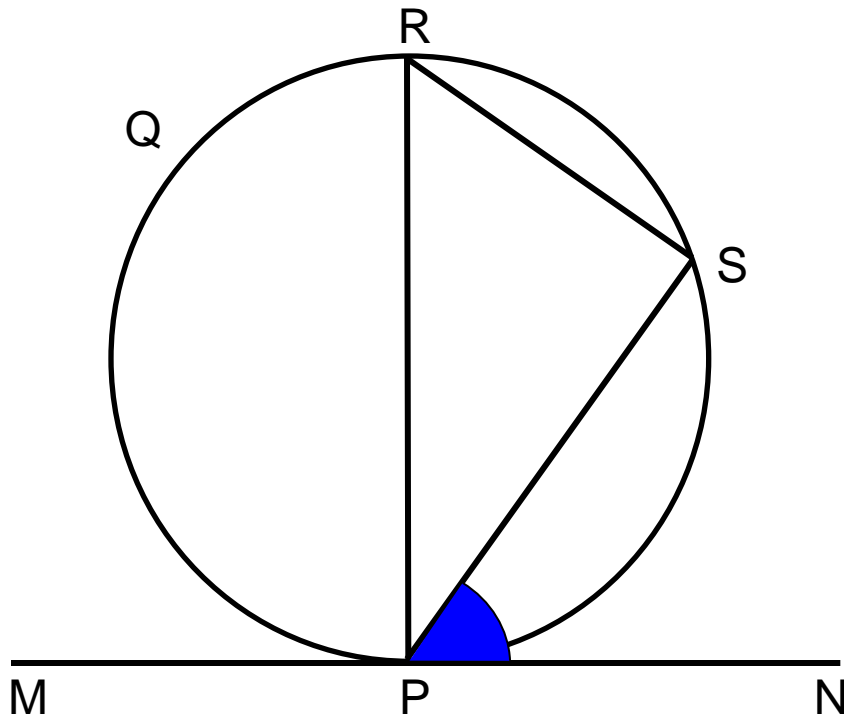
$$2(x + y) = 360^\circ$$

$$x + y = 180^\circ$$

Opposite Angles in Cyclic Quadrilateral are Supplementary

[Return to Menu](#)

# Alternate Segment Theorem



Given that

$MPN$  is a Tangent to the circle

$PS$  is a chord in the circle

Required to Prove

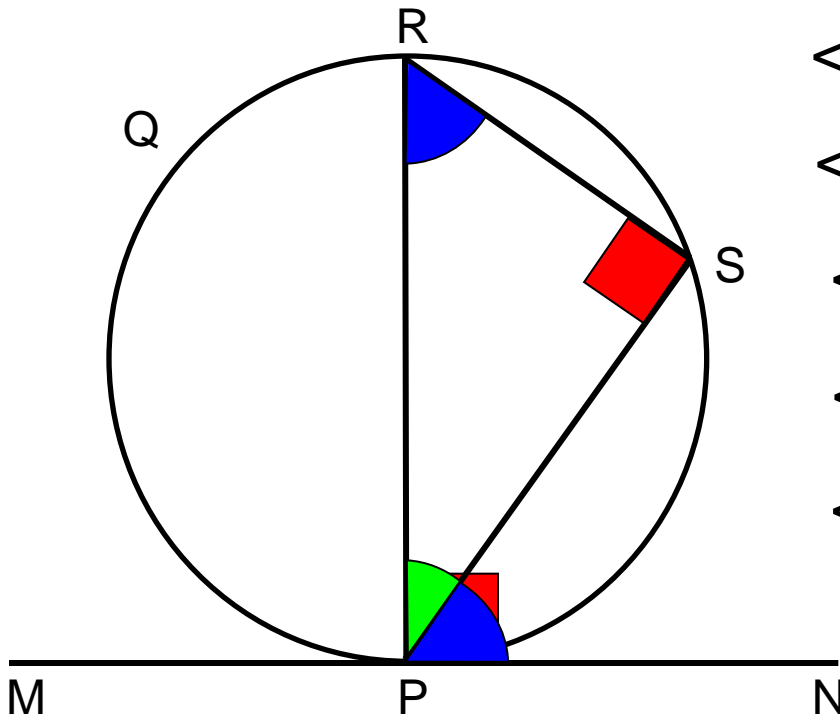
... that  $\angle SPN = \text{Any angle in the major segment } PQS$

Draw diameter  $PR$

Join  $RS$



# Alternate Segment Theorem



$\angle PSR = 90^\circ$  (Angle in Semicircle)

$\angle NPR = 90^\circ$  (Radius to a Tangent)

$\angle NPS + \angle RPS = 90^\circ$

$\angle PRS + \angle RPS = 90^\circ$

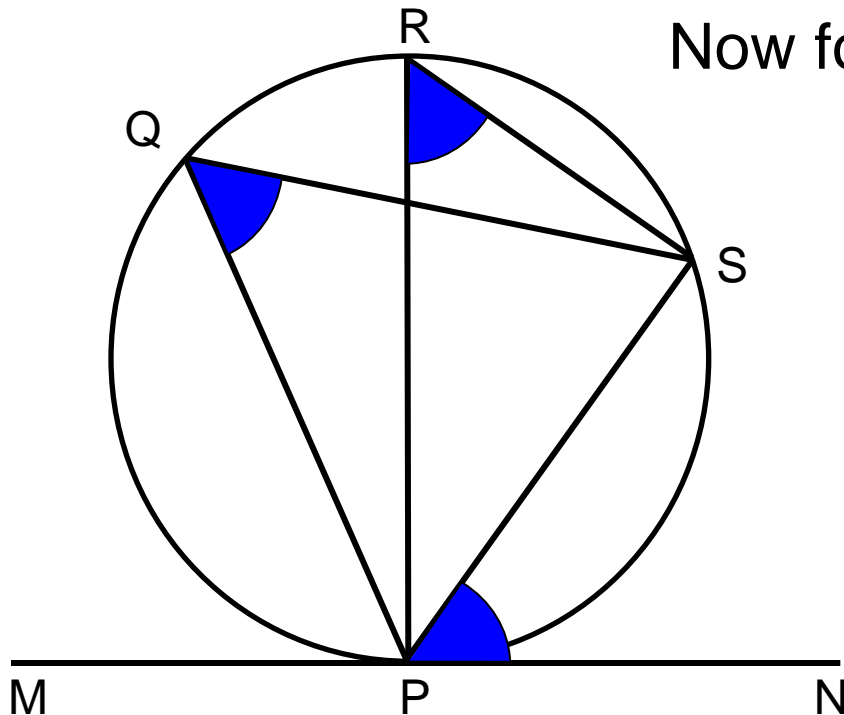
$\angle PRS + \angle RPS = \angle NPS + \angle RPS$

$\angle RPS$  is common

$\angle PRS = \angle NPS$

**Special case of Rightangle Triangle on circle's diameter**

# Alternate Segment Theorem



Now for ANY angle in Segment PQS

Join QS & PQ

Consider  $\angle PQS$

$\angle PQS = \angle PRS$

(Angles in SAME segment)

Thus  $\angle SPN = \text{Any Angle in Alternate Segment}$

[Return to Menu](#)